

Critical temperature, Critical Pressure, and Critical Volume

Critical temperature :->

It is defined as the temp. above which the gas cannot be liquified. It is denoted by T_c

Critical Pressure :->

The minimum pressure required to liquify the gas at the critical temperature is known as critical pressure. It is denoted by P_c .

Critical volume :->

The volume occupied by one mole of the gas at the critical temperature and critical pressure is called critical volume. It is denoted by V_c . The critical temperature, critical pressure and critical volume of a gas are collectively called as critical constant.

Relation between critical constant and Vander waal's constant

From Vander waal's equation we know that

$$\left(P + \frac{a}{V^2}\right)(V - b) = RT.$$

$$PV - Pb + \frac{a}{V} - \frac{ab}{V^2} = RT \quad \text{--- (1)}$$

on multiplying by V^2 and divided by P in equation (1) we get

$$V^3 - bV^2 + \frac{aV}{P} - \frac{ab}{P} = \frac{RT_c V^2}{P}$$

If $T = T_c$ and $P = P_c$, then

$$\text{or } V^3 - bV^2 - \frac{RT_c V^2}{P_c} + \frac{aV}{P_c} - \frac{ab}{P_c} = 0$$

$$V^3 - V^2 \left(b + \frac{RT_c}{P_c} \right) + \frac{aV}{P_c} - \frac{ab}{P_c} = 0 \quad \text{--- (II)}$$

Let $V = V_c$ then $(V - V_c) = 0$ or $(V - V_c)^3 = 0$

$$V^3 - V_c^3 - 3VV_c(V - V_c) = 0$$

$$V^3 - V_c^3 - 3V_c V^2 - 3V_c^2 V = 0 \quad \text{--- (III)}$$

Comparing equation (II) and (III)

$$3V_c = b + \frac{RT_c}{P_c} \quad \text{--- (IV)}$$

$$3V_c^2 = \frac{a}{P_c} \quad \text{--- (V)}$$

$$V_c^3 = \frac{ab}{P_c} \quad \text{--- (VI)}$$

On dividing equation (V) in eqn (VI)

$$\frac{V_c^3}{3V_c^2} = \frac{ab}{P_c} \cdot \frac{1}{a/P_c} \quad \text{So } V_c = 3b \quad \text{--- (VII)}$$

From equation (IV) and (VII) Putting this value in eqn (IV)

$$3(3b)^2 = \frac{a}{P_c}$$

$$3 \times 9b^2 = \frac{a}{P_c}$$

$$27b^2 = \frac{a}{P_c} \quad \therefore P_c = \frac{a}{27b^2}$$

Put the value of V_c in P_c in equation (IV)

$$3 \times 3b = b + \frac{RT_c}{a/27b^2}$$

$$9b = b + RT_c \times 27b^2$$

$$8b = \frac{RT_c \times 27b^2}{a} \quad \therefore T_c = \frac{8a}{27Rb}$$